

Evaluate the Integral

$$1) \int \sin^3 x \cos^2 x dx \quad \boxed{\frac{1}{5} \cos^5 x - \frac{1}{3} \cos^3 x + C}$$

$$2) \int \sin^6 x \cos^3 x dx \quad \boxed{\frac{1}{7} \sin^7 x - \frac{1}{9} \sin^9 x + C}$$

$$3) \int_0^{\pi/2} \cos^5 x dx \quad \boxed{\frac{8}{15}}$$

$$4) \int \sin^3(mx) dx \quad \boxed{\frac{1}{3m} \cos^3(mx) - \frac{1}{m} \cos(mx) + C}$$

$$5) \int_0^{\pi/2} \cos^2 \theta d\theta$$

$\frac{\pi}{4}$

$$6) \int_0^{\pi} \sin^4(3t) dt$$

$\frac{3\pi}{8}$

$$7) \int (1 + \cos \theta)^2 d\theta$$

$\frac{3}{2}\theta + 2\sin \theta + \frac{1}{4}\sin 2\theta + C$

$$8) \int x \cos^2 x dx$$

$\frac{1}{4}x^2 + \frac{1}{4}x \sin 2x + \frac{1}{8}\cos 2x + C$

$$9) \int_0^{\pi/2} \sin^2 x \cos^2 x dx \quad \boxed{\frac{\pi}{16}}$$

$$10) \int \sin^3 x \sqrt{\cos x} dx \quad \boxed{\frac{2}{7}(\cos x)^{7/2} - \frac{2}{3}(\cos x)^{3/2} + C}$$

$$11) \int \cos \theta \cos^5(\sin \theta) d\theta \quad \boxed{\sin(\sin \theta) - \frac{2}{3}\sin^3(\sin \theta) + \frac{1}{5}\sin^5(\sin \theta) + C}$$

$$12) \int \cos^2 x \tan^3 x dx \quad \boxed{\frac{1}{2}\cos^2 x - \ln|\cos x| + C}$$

$$13) \int \frac{1-\sin x}{\cos x} dx$$

$$\boxed{\ln(1+\sin x) + C}$$

$$14) \int \sec^2 x \tan x dx$$

$$\boxed{\frac{1}{2} \tan^2 x + C}$$

$$15) \int \sec^6 t dt$$

$$\boxed{\frac{1}{5} \tan^5 t + \frac{2}{3} \tan^3 t + \tan t + C}$$

$$16) \int \tan^3(2x) \sec^5(2x) dx$$

$$\boxed{\frac{1}{14} \sec^7(2x) - \frac{1}{10} \sec^5(2x) + C}$$

$$17) \int \frac{\tan^3 \theta}{\cos^4 \theta} d\theta$$

$$\boxed{\frac{1}{6} \tan^6 \theta + \frac{1}{4} \tan^4 \theta + C}$$

$$18) \int_{\pi/6}^{\pi/2} \cot^2 x dx$$

$$\boxed{\frac{\pi}{3}}$$

$$19) \int \csc^4 x \cot^6 x dx$$

$$\boxed{-\frac{1}{9} \cot^9 x - \frac{1}{7} \cot^7 x + C}$$

$$20) \int \csc x dx$$

$$\boxed{\ln |\csc x - \cot x| + C}$$

$$21) \int \sin(5x) \sin(2x) dx$$

$$\boxed{\frac{1}{6} \sin 3x - \frac{1}{14} \sin 7x + C}$$

$$22) \int \sin(3x) \cos x dx$$

$$\boxed{-\frac{1}{8} \cos 4x - \frac{1}{4} \cos 2x + C}$$

$$23) \int \frac{dx}{\cos x - 1}$$

$$\boxed{\csc x + \cot x + C}$$